

# Temperature dissemination in a post-redefinition world

Dr. Patrick Rourke, National Research Council Canada

29<sup>th</sup> Meeting of the CCT – Session 2

4 November 2020



## Review

# The revision of the SI—the result of three decades of progress in metrology

Michael Stock<sup></sup>, Richard Davis<sup></sup>, Estefanía de Mirandés  
and Martin J T Milton<sup></sup>

Bureau International des Poids et Mesures, BIPM, Pavillon de Breteuil, 92310 Sèvres, France



**THE KELVIN IS  
DEAD,  
LONG LIVE THE  
KELVIN!**

# The redefinition of the kelvin – what's next?

The CCT Declaration of 2014 acknowledges the known short-comings of both defined temperature scales (CCT 2014)

- For the ITS-90: ‘inherent weaknesses, including known discrepancies from  $T$ ’.
- For the PLTS-2000: ‘currently no resolution of its inherent discrepancy of ~6 % at the lowest temperatures’.

and concludes that new thermodynamic temperature determinations are required to support:

- ‘In the short term: the introduction and implementation of the *mise en pratique* of the definition of the kelvin ( $MeP-K$ ) through determining robust, reliable values of  $T-T_{90}$  and  $T-T_{2000}$ ’.
- ‘In the medium term: facilitate direct dissemination of the redefined kelvin through developing robust and reliable methodologies to disseminate  $T$ , particularly at the extremes of temperature  $>1300$  K and  $<1$  K’.
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## Primary thermometers

- $T$ : Thermodynamic temperature

## Defined scales $T_{\text{scale}}$ (approximations to $T$ )

- $T_{90}$ : International Temperature Scale of 1990 (ITS-90)
- $T_{2000}$ : Provisional Low Temperature Scale of 2000 (PLTS-2000)
- $T_{XX}$ : Future temperature scale (ITS-XX)

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SI Brochure – 9th edition (2019) – Appendix 2

20 May 2019

In the future, as the primary methods evolve and are expected to achieve lower uncertainties, primary thermometers will become more widely used and gradually replace the ITS-90 and the PLTS-2000 as the basis of temperature measurement.

- $< 1\text{K} \rightarrow \text{middle} \leftarrow > 1300\text{K}$
- Global transition likely messy and incomplete, smeared out in:
  - Time
  - Space
  - Temperature range
  - Position in calibration chain
- **Mixed dissemination environment**

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Metrologia 57 (2020) 035003 (23pp) <https://doi.org/10.1088/1681-7575/ab6b3c>

## Standard platinum resistance thermometer interpolations in a revised temperature scale

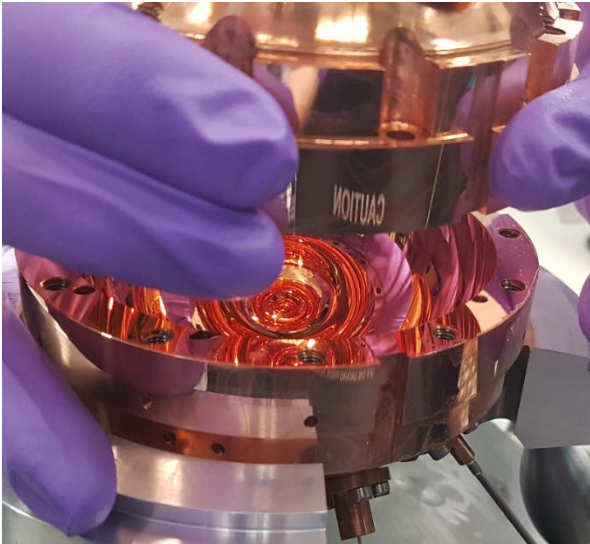
D R White<sup>1</sup> and P M C Rourke<sup>2</sup>

<sup>1</sup> Measurement Standards Laboratory, Lower Hutt PO Box 31310, New Zealand  
<sup>2</sup> National Research Council, 1200 Montreal Rd., Ottawa, Ontario, Canada

### Scale attributes (separable!):

- **Reproducibility**
- **Thermodynamic Accuracy**

# Temperature dissemination in a post-redefinition world



## OUTLINE

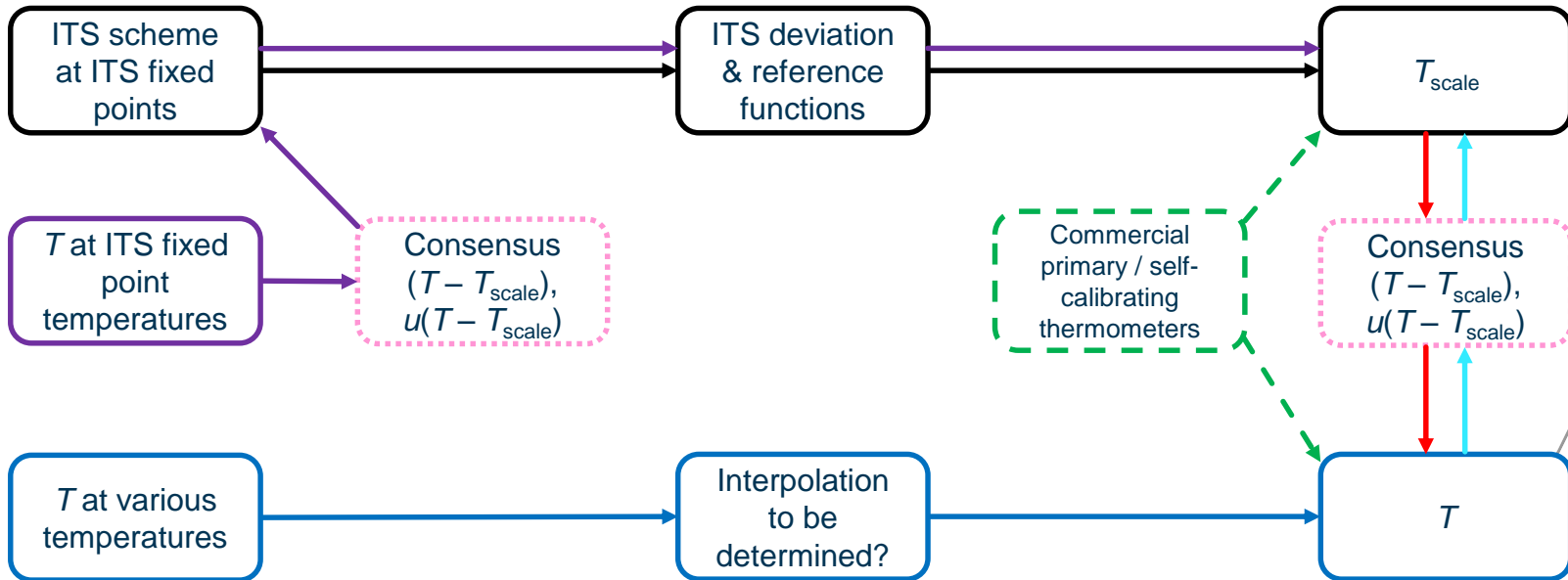
- Routes to dissemination
- Reproducibility:  $T_{90}$  vs.  $T_{XX}$  vs.  $T$
- Dissemination path examples
- Thermodynamic inaccuracy of the ITS-90
- KCs and CMCs for primary thermometers
- Further  $T$  dissemination issues
- Summary and discussion

# Routes to dissemination

## CALIBRATION

## INTERPOLATION & CONVERSION

## REALIZATION



# Reproducibility: $T_{90}$ vs. $T_{XX}$ vs. $T$

## ILLUSTRATIVE EXAMPLE

- Capsule standard platinum resistance thermometer (CSPRT) calibration:  $T_{90}$ ,  $T_{XX}$ ,  $T$
- Triple point of equilibrium hydrogen at 13.8033 K to triple point of water at 273.16 K
- NRC CSPRT comparison block data set, direct calculations from experimental measurements:
  - Type 1 non-uniqueness (subrange inconsistency “SRI”)
  - Type 3 non-uniqueness (artifact dependence “NU3”)
  - Propagation of uncertainties from fixed points (“PoU”)



**ITS-90 reproducibility, xenon fixed point substitution and new interpolating equations between 13.8033 K and 273.16 K**

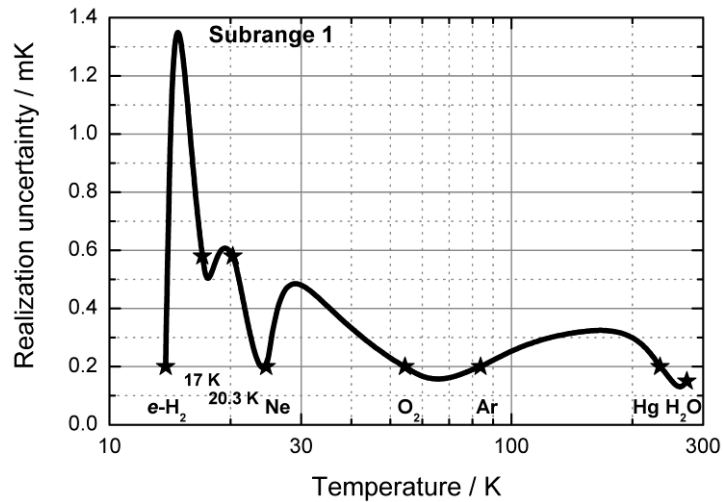
*(To be submitted)*

**P M C Rourke**

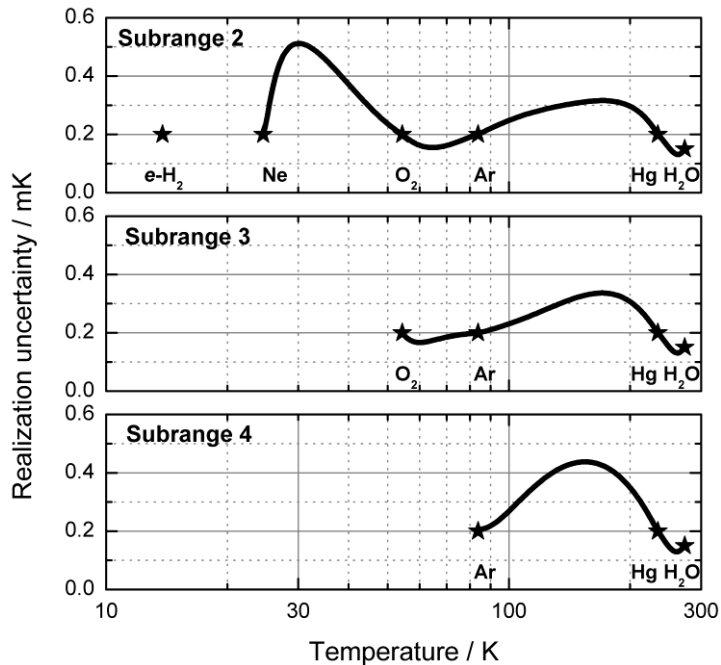
National Research Council, 1200 Montreal Road, Ottawa, ON, K1A 0R6 Canada



# Reproducibility: $T_{90}$



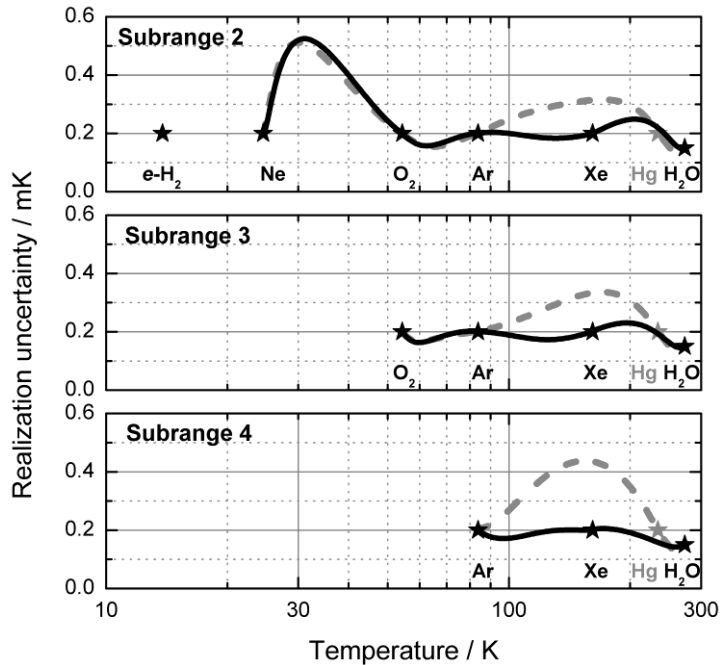
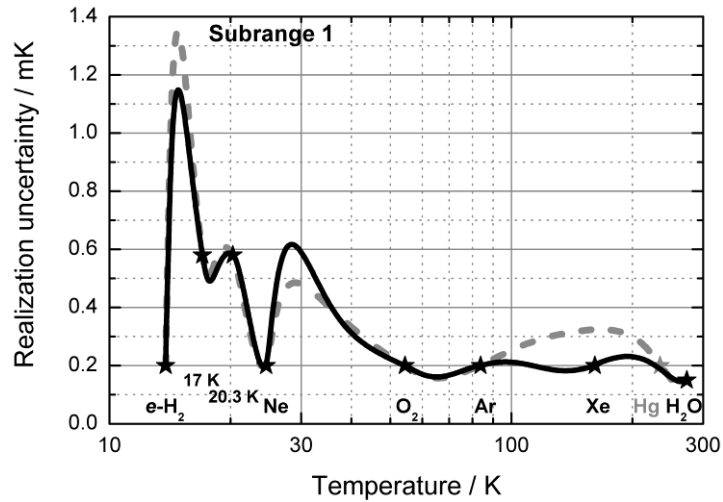
—  $T_{90}$  dissemination (NRC)



## NRC $k = 1$ CSPRT calibration uncertainties

- 0.15 mK @ TPW
- 0.20 mK @ Hg, Ar, O<sub>2</sub>, Ne & e-H<sub>2</sub>
- 0.58 mK @ 20.3 K & 17 K
- Hill *et al.* "CCT-K2.5 Final Report" 2015

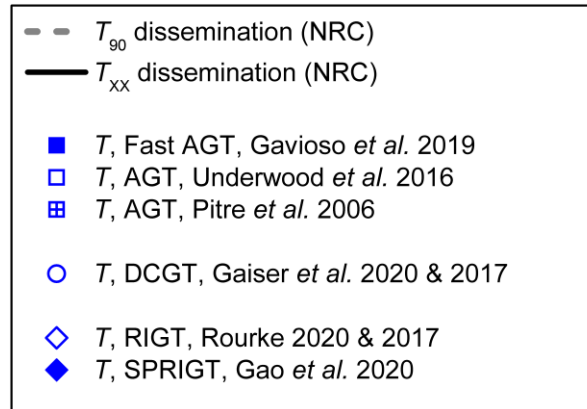
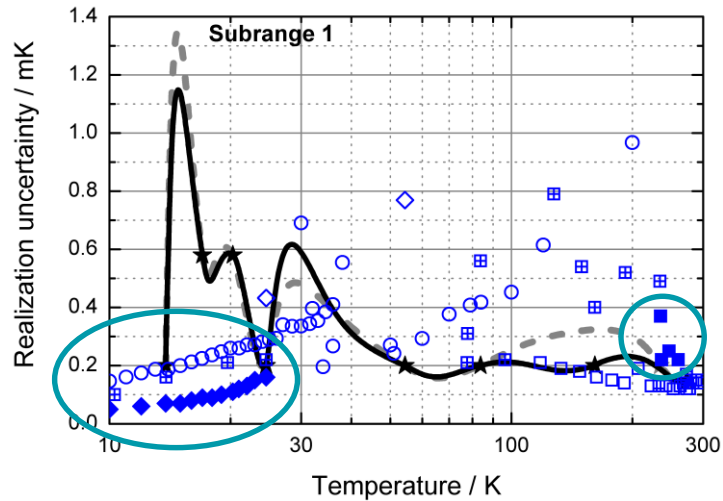
# Reproducibility: $T_{90}$ vs. $T_{XX}$



## ITS-XX “Lite”

- Xenon replaces mercury
- New deviation functions for subranges 1, 2 & 3
- Same reference function as ITS-90
- More reproducible scale, same thermodynamic inaccuracy
- Minimally disruptive?

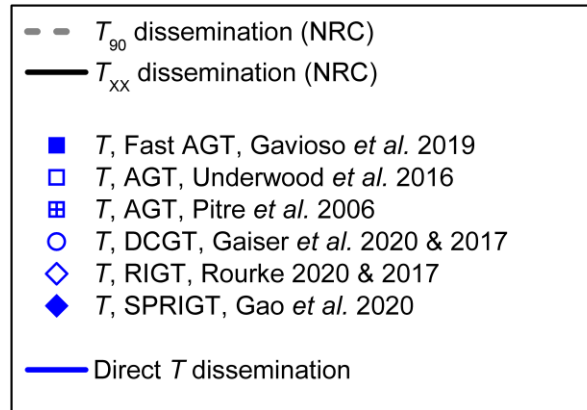
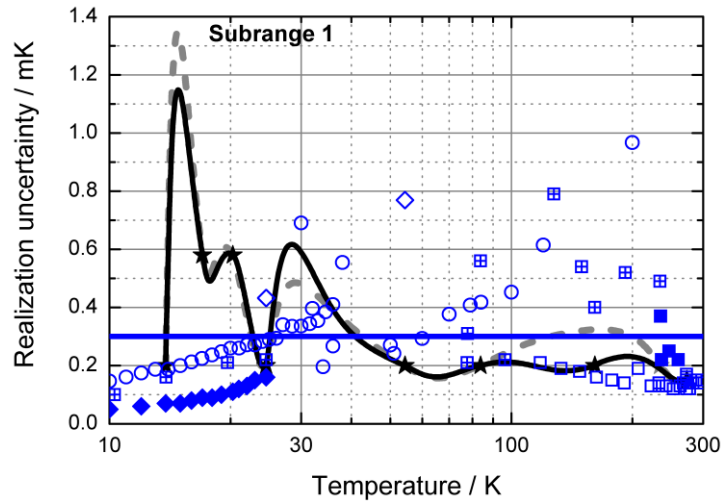
# Reproducibility: $T_{90}$ vs. $T_{XX}$ vs. $T$



$u(T)$

- Multiple techniques
- “Fast” methods
- Consistent low-temperature performance

# Dissemination path examples: direct $T$ dissemination



## Direct $T$ dissemination

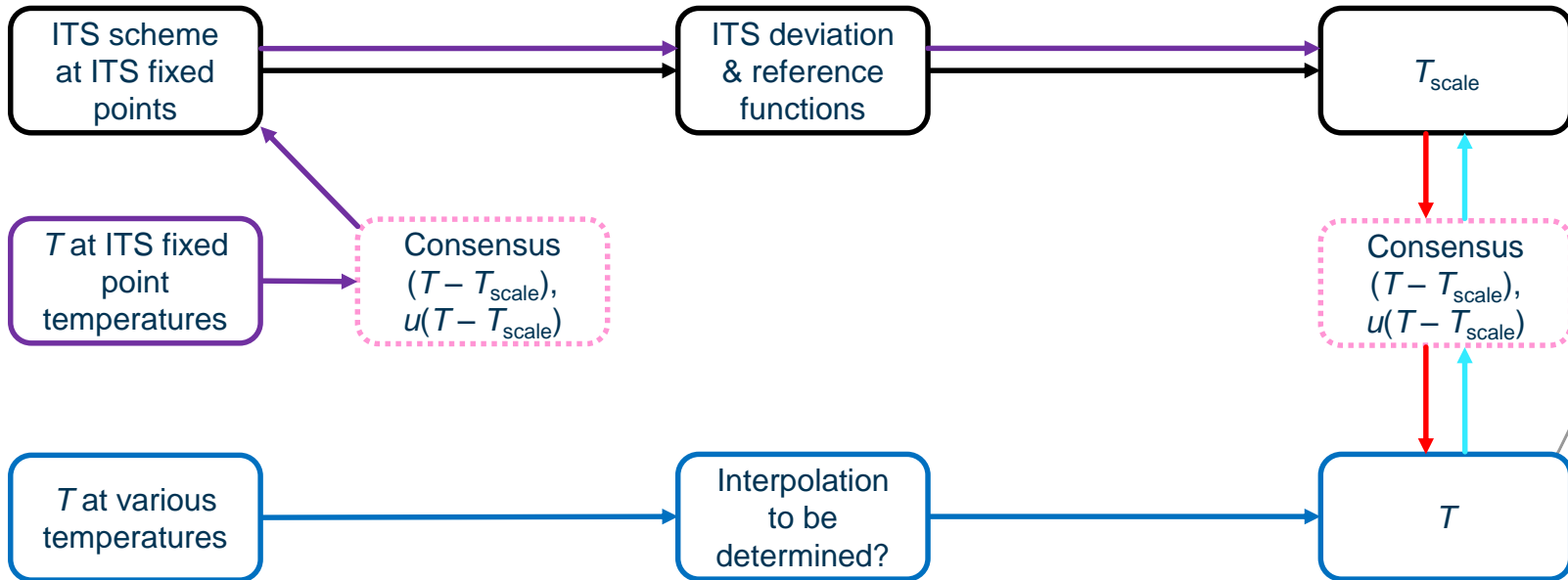
- Research vs. calibration
- $u(T) \sim 0.3$  mK likely attainable for dissemination with near-future technology

# Dissemination path examples

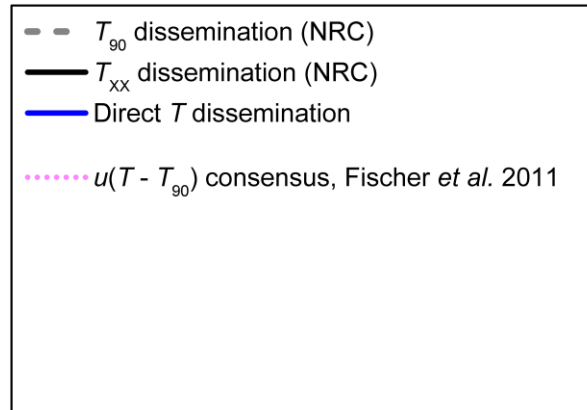
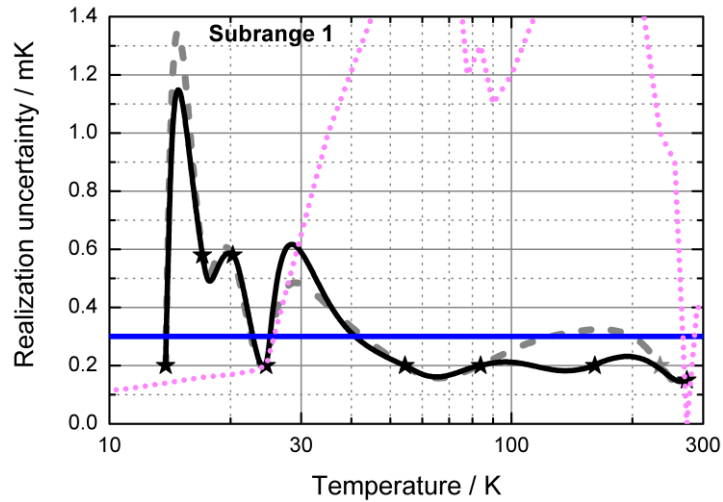
## CALIBRATION

## INTERPOLATION & CONVERSION

## REALIZATION



# Dissemination path examples: conversion using $(T - T_{\text{scale}})$ & $u(T - T_{\text{scale}})$



## Community consensus 2011

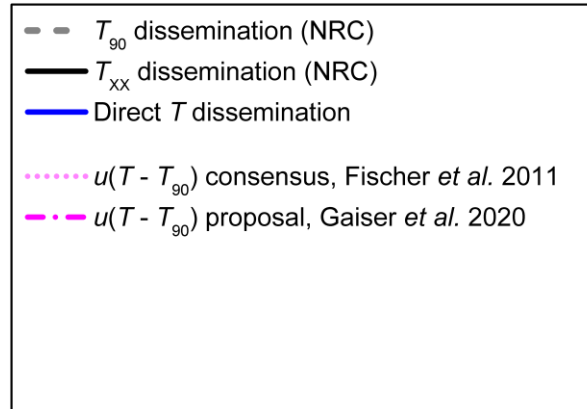
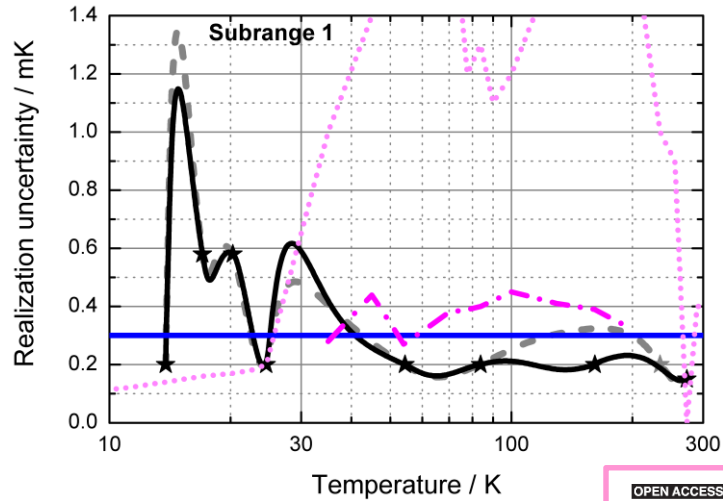
- $(T - T_{90})$
- $u(T - T_{90})$

Int J Thermophys (2011) 32:12–25  
DOI 10.1007/s10765-011-0922-1

### Present Estimates of the Differences Between Thermodynamic Temperatures and the ITS-90

J. Fischer · M. de Podesta · K. D. Hill ·  
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# Dissemination path examples: conversion using $(T - T_{\text{scale}})$ & $u(T - T_{\text{scale}})$



## Community consensus

- Experimental work on-going worldwide, over entire temperature range of defined scales
- More reliable consensus ( $T - T_{90}$ ) imminent?
- Gaiser *et al.* 2020
- CCT-WG-CTh
- 4 K to 303 K or 430 K?


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Metrologia

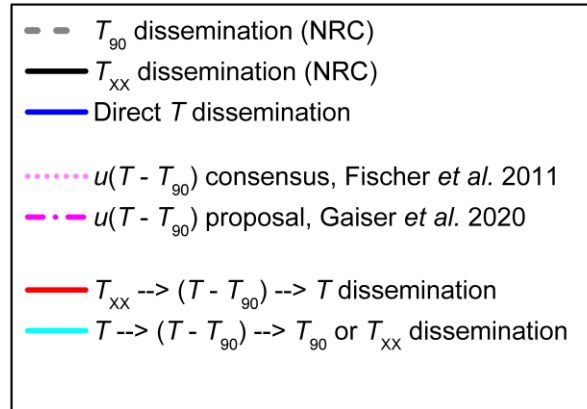
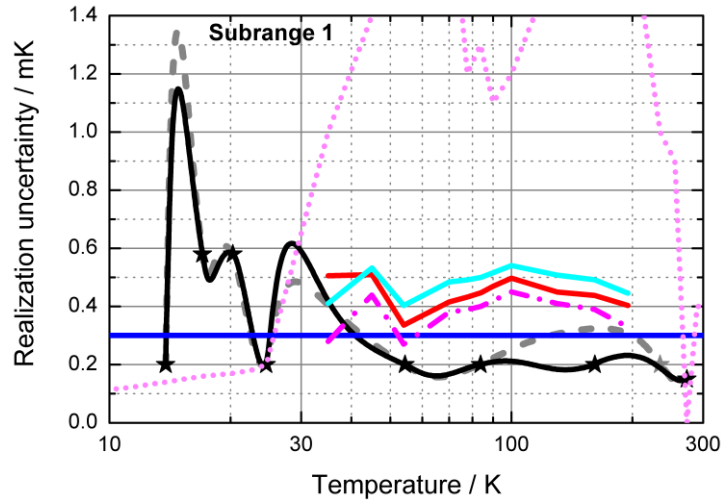
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## Thermodynamic-temperature data from 30 K to 200 K

Christof Gaiser , Bernd Fellmuth and Norbert Haft

Physikalisch-Technische Bundesanstalt (PTB), Abbestrasse 2-12, 10587 Berlin, Germany

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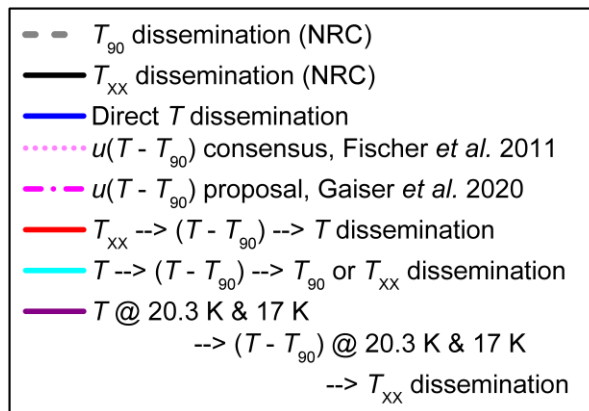
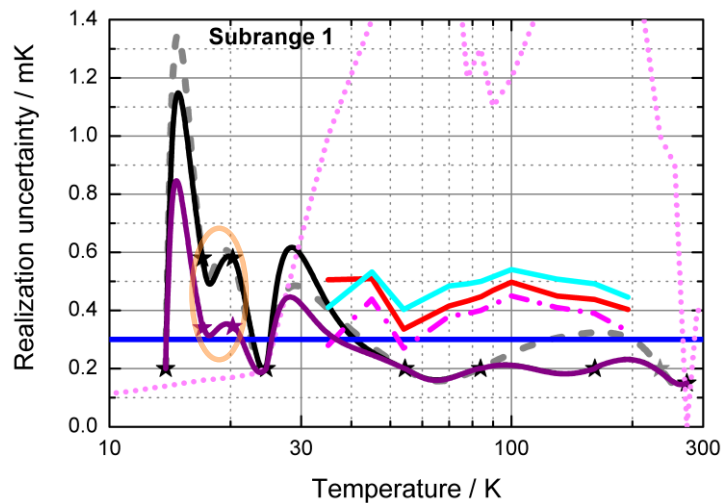


$T_{\text{scale}} \rightarrow T$

$T \rightarrow T_{\text{scale}}$



# Dissemination path examples: $T$ punch in at defined scale fixed point(s)

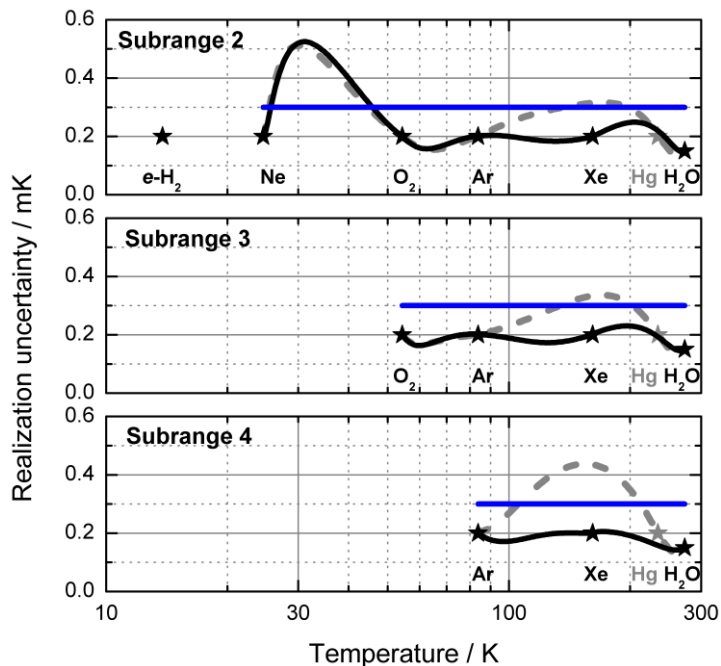
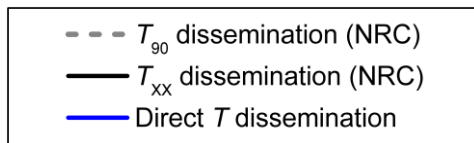
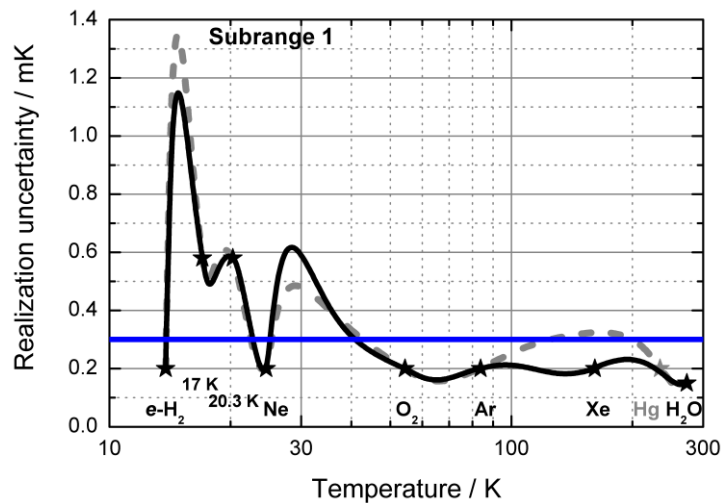


$$T_{\text{scale}} \rightarrow T$$

$$T \rightarrow T_{\text{scale}}$$

- Primary thermometers may replace:
  - Interpolating gas thermometers (IGTs)
  - Hydrogen vapour pressure (e-H<sub>2</sub> VP) systems
  - Other fixed points?

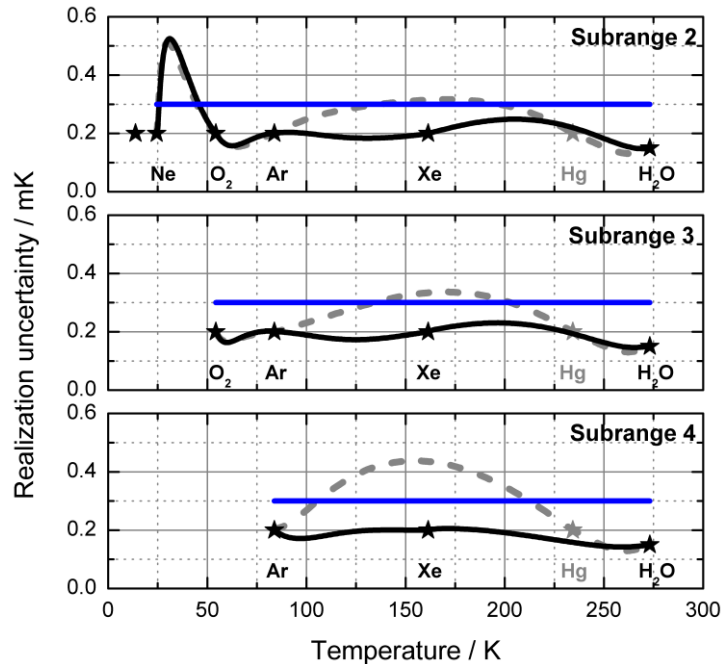
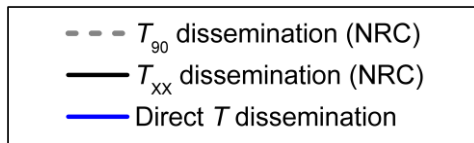
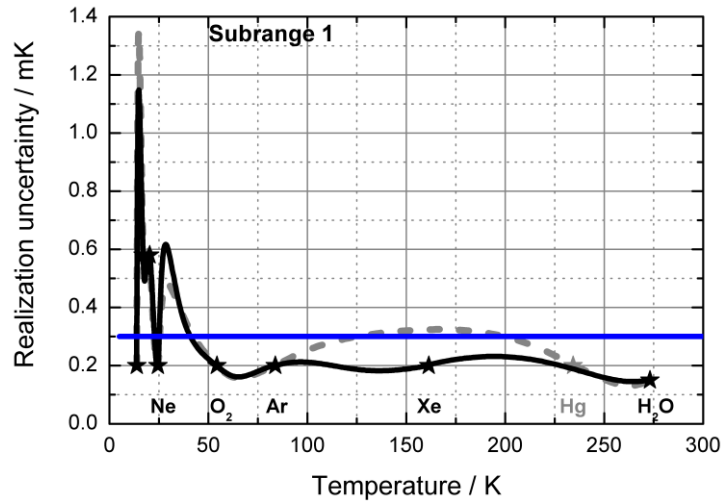
# Dissemination path examples



**Reproducibility of direct  $T$  competitive with defined scale**

- Up to 24.5 K
- IGTs / e-H<sub>2</sub> VP systems already cumbersome
- Looks good in 24.5 K to 54 K range too

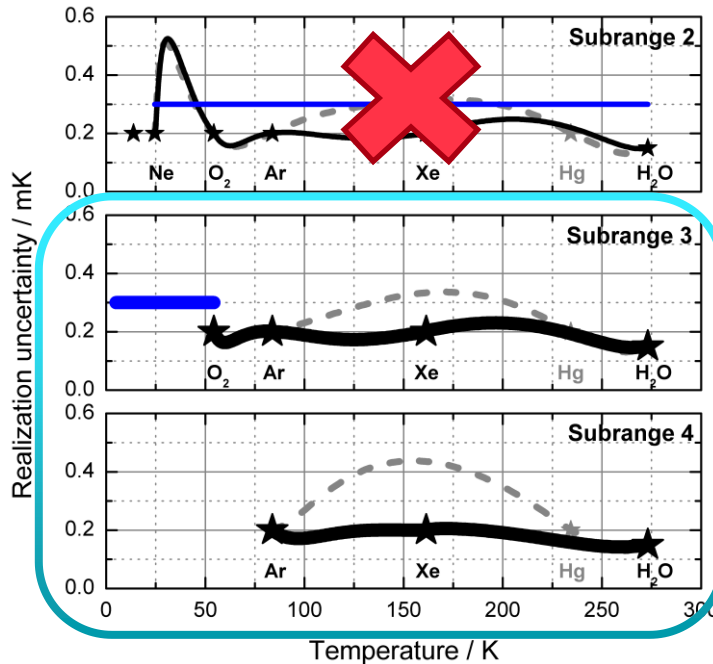
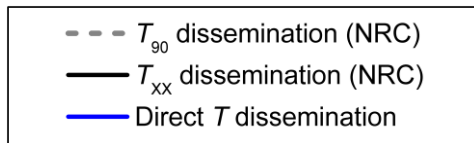
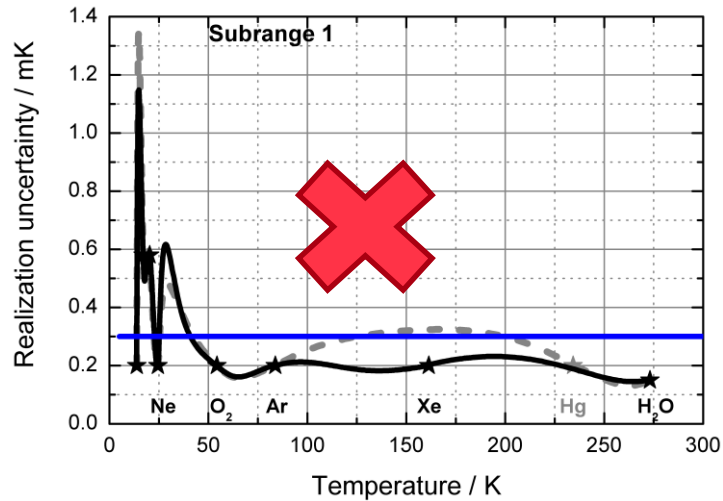
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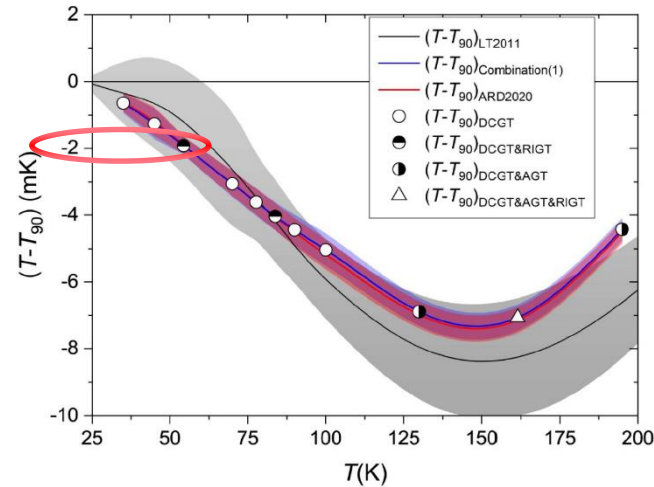
# Optimum reproducibility approach



**Dissemination:**  
 $T < 54 \text{ K}$ ,  $T_{xx} > 54 \text{ K}$

- Primary thermometry displaces ITS subranges 1 & 2
- ITS-XX “Lite” subranges 3 & 4 have excellent reproducibility, need few calibration points
- Changeover at the triple point of oxygen
- But...

# Thermodynamic inaccuracy of the ITS-90



## ITS-90 is a poor approximation to thermodynamic temperature

- 2 mK discrepancy at 54 K =  $10 \times u_{\text{NRC}}(T_{90})$
- Big step change if dissemination switches from  $T$  to approximation-to- $T$  (defined scale) here
- Cross-converting incurs additional uncertainty
- Even worse at 84 K and beyond
- Problem may become pervasive, unless:
  - Direct dissemination of the kelvin according to its new definition is confined to temperature regions where  $T_{\text{scale}} \approx T$ ; or
  - Thermodynamic accuracy of defined scales are improved

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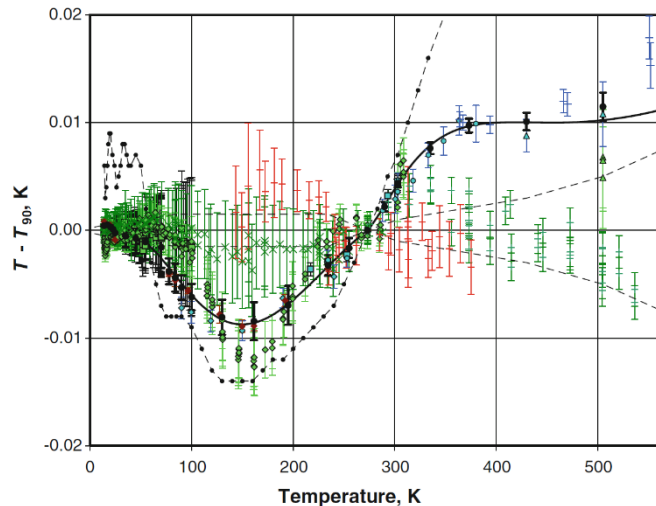
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NATIONAL RESEARCH COUNCIL CANADA

## At higher temperatures too

- $(T - T_{90}) \approx 400 \text{ mK} = 0.4 \text{ K}$  at  $3000 \text{ }^\circ\text{C}$
- Second radiation constant  $c_{2,90} \neq c_2 \equiv hc/k$
- Non-uniqueness of the ITS-90  $\approx 100 \text{ mK} = 0.1 \text{ K}$  at  $3000 \text{ }^\circ\text{C}$

All are now defined  
constants of the SI

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Metrologia 57 (2020) 045007 (7pp)

Metrologia

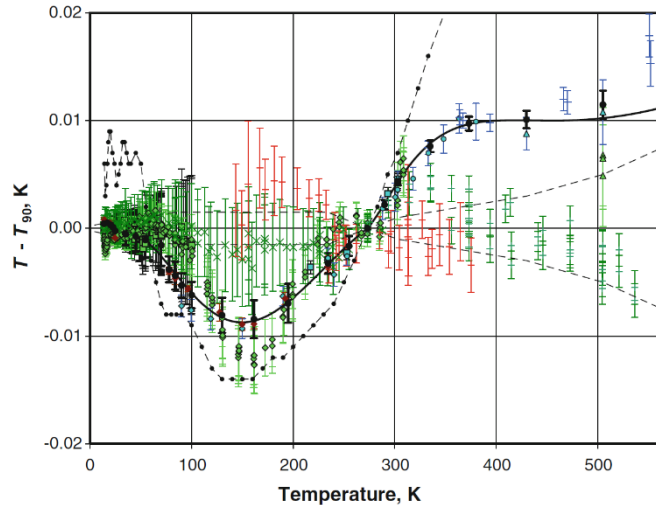
<https://doi.org/10.1088/1681-7575/e045007>

**The non-uniqueness of ITS-90 above the  
silver point and its impact on values of  
 $T - T_{90}$**

Peter Saunders

Measurement Standards Laboratory of New Zealand, PO Box 31-310, Lower Hutt, New Zealand

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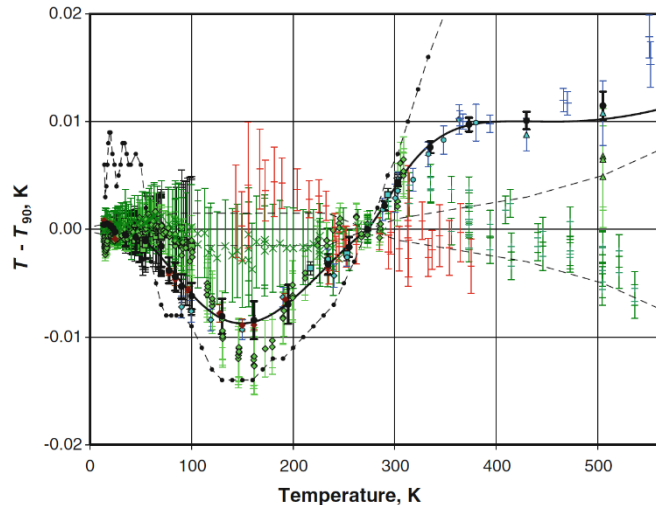
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- Dissemination patchwork:
  - Time
  - Space
  - Temperature range
  - Position in calibration chain
- Mixed dissemination environment
- **Danger of confusion between  $T$  and  $T_{90}$  in broader downstream community**

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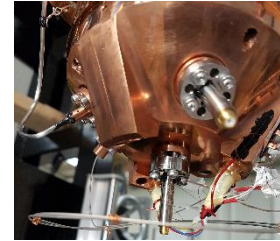
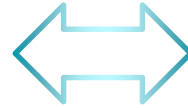
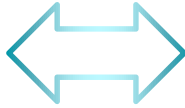
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  - Time
  - Space
  - Temperature range
  - Position in calibration chain
- Mixed dissemination environment
- **Danger of confusion between  $T$  and  $T_{90}$  in broader downstream community**
- **Cost of confusion vs. cost of new scale?**
- Metrology  $\Rightarrow$  applications



# KCs and CMCs for primary thermometers: beware pre-ITS-style laboratory scales!



## Key Comparisons

- Exchanging primary thermometers unfeasible
- SPRTs as transfer standards?
  - What if reproducibility / stability of primary thermometers eclipses SPRTs?
  - *E.g.* improvement: lamps → radiation thermometers
- Additional uncertainty:  $T \leftrightarrow T_{\text{scale}}$

## Calibration and Measurement Capabilities

- Non-contact thermometry leading the way
  - Simultaneously handle CMC review process for  $T_{\text{scale}}$  &  $T$
  - Higher uncertainties
  - Manageable NMI workload
- Commercial primary / “self-calibrating” thermometers?

# Further $T$ dissemination issues

## To think about...

- Implications for core industrially-relevant long-stem SPRT range: triple point of argon (84 K) to freezing point of aluminum (660 °C)
- Calibration points, interpolation, non-uniqueness, propagation of uncertainty
  - Prescribed for defined scales; limited number of cal. points / subranges
  - Direct  $T$  dissemination cal. points & interpolation could be anything
  - More complicated if new interpolating instruments begin to be used at the highest levels (Task Group on Emerging Technologies!)
- What if primary thermometers not meeting criteria for inclusion in the *MeP-K* begin to be used “in the wild”?



LSPRTs on the way to NIST for CCT-K9

# Summary and discussion



The redefinition  
of the kelvin –  
what's next?

## Mixed $T_{\text{scale}}$ and $T$ dissemination world

- ITS-XX “Lite” more reproducible than ITS-90, same thermodynamic inaccuracy, low disruption
- Near future  $T$  dissemination: reproducibility likely competitive with defined scales up to 54 K
- Costs of downstream  $T$  &  $T_{\text{scale}}$  confusion vs. disruption of introducing thermodynamically-accurate ITS-XX “Deluxe”
- Better metrology enables new applications & technologies
- Primary thermometers:
  - Key Comparisons & Calibration and Measurement Capabilities
  - Implications for industrially-relevant 84 K to 660 °C LSPRT range
  - Calibration points, interpolation, non-uniqueness, propagation of uncertainty



# THANK YOU

Patrick Rourke • [patrick.rourke@nrc-cnrc.gc.ca](mailto:patrick.rourke@nrc-cnrc.gc.ca)

