BIPM Workshop "The Quantum Revolution in Metrology" 28-29 September, 2017, Sèvres, France

## Error modelling of quantum Hall array resistance standards

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## Introduction

Quantum Hall array resistance standards (QHARS) are integrated devices composed of interconnected quantum Hall effect elements that allow the realization of arbitrary resistance values. The evaluation of the accuracy of a QHARS is an open problem, because of the effect of the contact and wire resistances.

We present here a general and systematic procedure for the error modelling of QHARSs, based on modern circuit analysis techniques and Monte Carlo evaluation of the uncertainty.

This method of analysis is applied, as example, to the characterization of a 1 M $\Omega$ QHARS fabbricated by the National Metrology Institute of Japan.

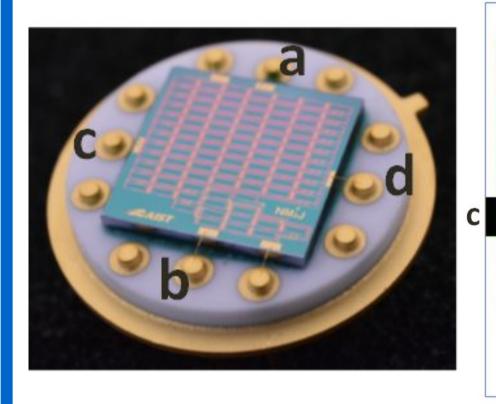


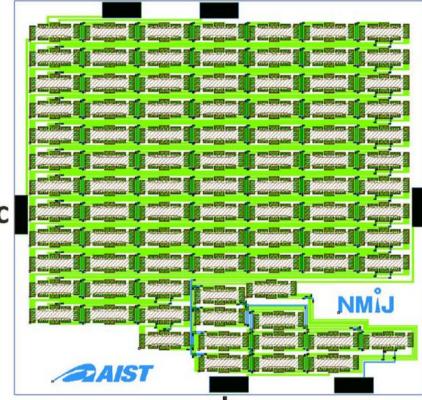
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## 1 MΩ QHARS

The 88 Hall bars were fabricated on a 8mm-GaAs/AlGaAs square chip using triple connection technique.





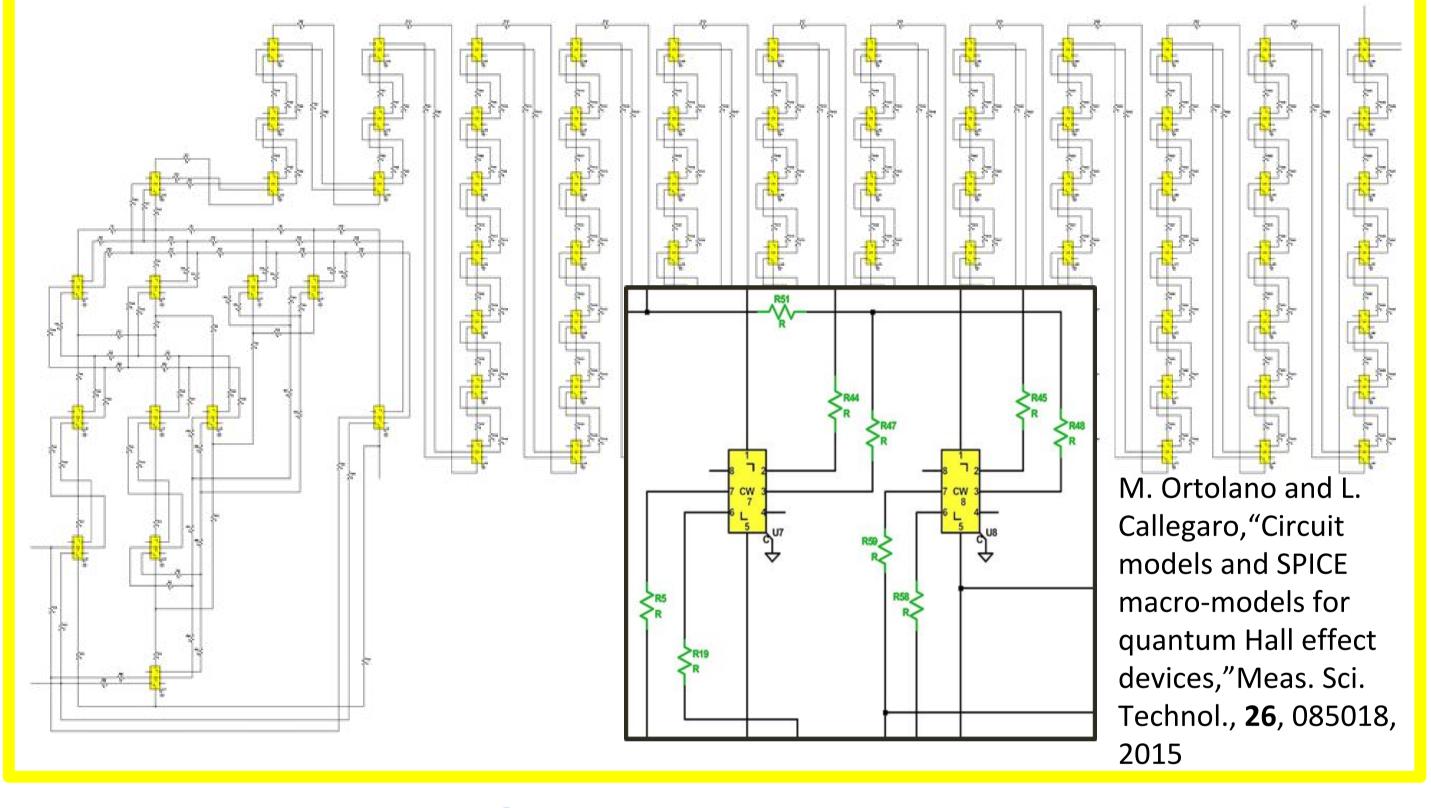
of 1 M $\Omega$ Quantum Hal Array Resistance Standards", **IEEE Trans.** Instrum. Meas., **66**, 1475, 2017.

T. Oe et al.,

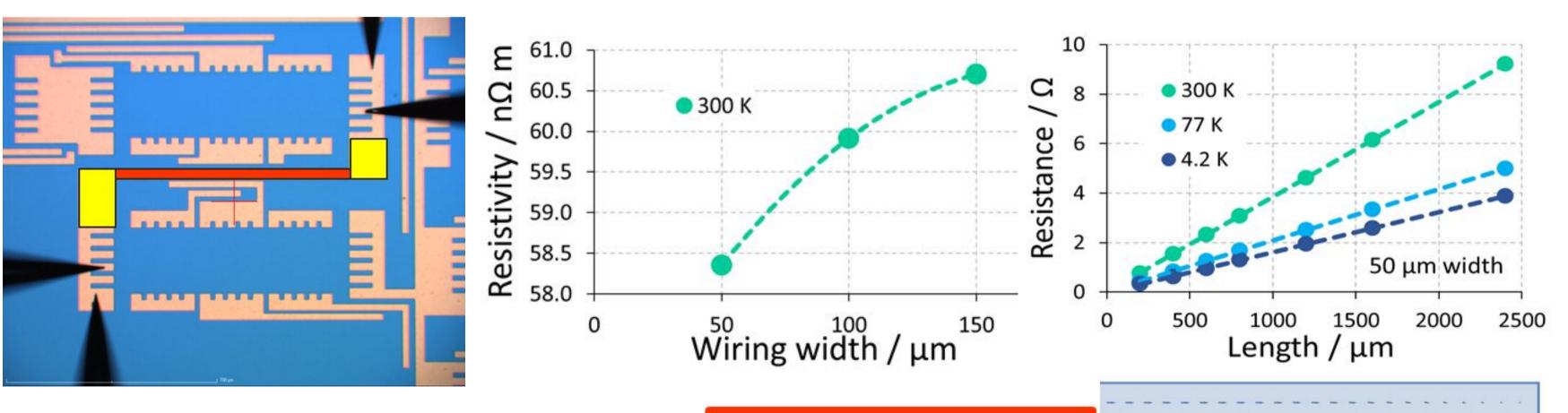
"Development

**QHARSmachine Workflow** 

LTspice  $\{a,b,c,d\}$ schematic editor LTspice schematic QHARSmachine endpoint Converter Annotated schematic Matrix  $\boldsymbol{A}$ 1.5 1.0 Stray parameters Stray parameters Excel spreadsheet LTspice Solver simulator Stray parameters sample item Simulated probability Item deviation distribution of  $\Delta R_{ab,cd}^{\rm Q}$ for cross-checking LTspice schematic 1  $M\Omega$  QHARS

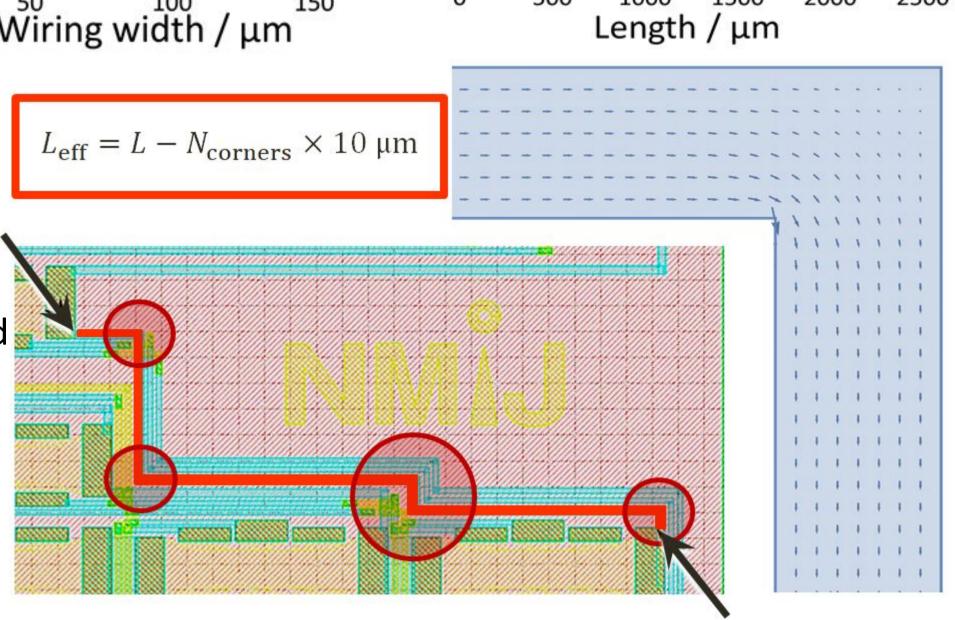


## Wire resistances evaluation

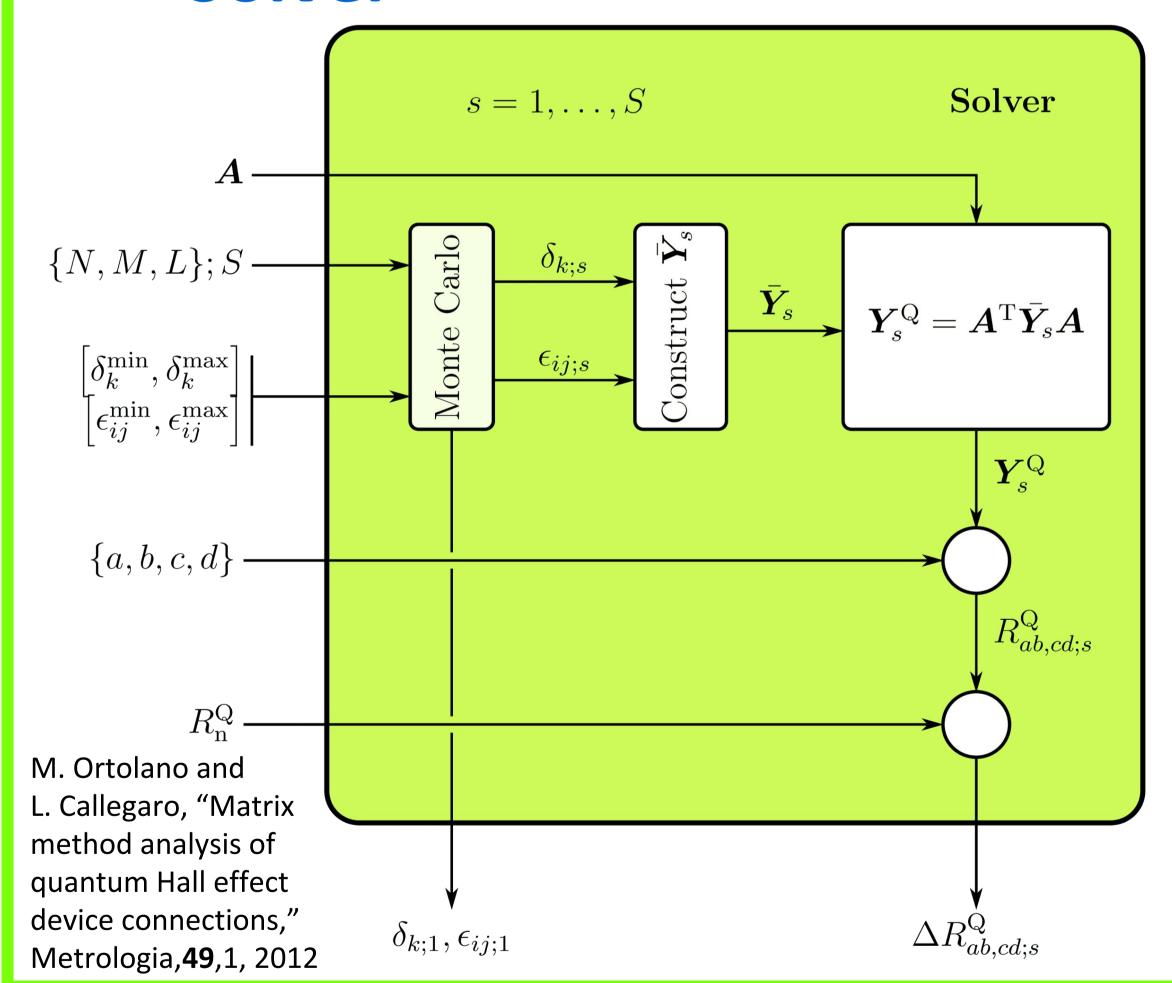


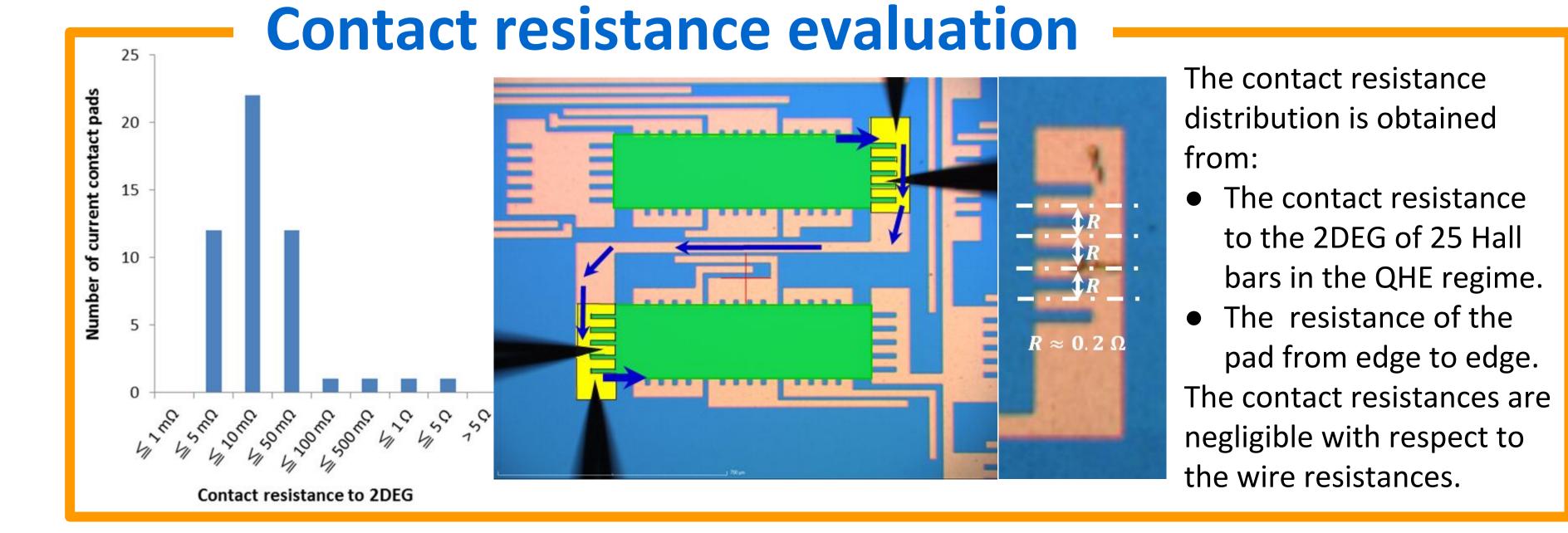
• The resistivity at 4K of 50  $\mu$ m wide wires is measured by using a test pattern. Then by fitting the resistivity obtained at RT, we scaled the resistivity at 4K for each segment width.

We introduced a correction factor to account for the reduced resistance due to elbows along the current wires. This factor has been obtained by a finite elements simulation.



Solver





Result  $\delta R_{\rm ab,cd}^{\rm Q} \approx 3.5 \times 10^{-11}$   $u(\delta R_{\rm ab,cd}^{\rm Q}) \approx 1 \times 10^{-12}$ 100 20 3.6 3.7  $10^{11} \times \delta R_{\rm ab,cd}^{\rm Q}$